## Exercise 76

A cell phone company offers two plans for minutes.

- Plan A: $\$ 15$ per month and $\$ 2$ for every 300 texts
- Plan B: $\$ 25$ per month and $\$ 0.50$ for every 100 texts

How many texts would you need to send per month for plan B to save you money?

## Solution

The cost in Plan A is

$$
C_{A}(x, m)=15 m+\frac{2}{300} x,
$$

and the cost in Plan B is

$$
C_{B}(x, m)=25 m+\frac{0.50}{100} x,
$$

where $x$ is the number of texts sent and $m$ is the number of months the plan is bought for. Find where Plan A is more expensive than Plan B.

$$
\begin{gathered}
C_{A}(x, d)>C_{B}(x, d) \\
15 m+\frac{2}{300} x>25 m+\frac{0.50}{100} x \\
\frac{2}{300} x-\frac{0.50}{100} x>25 m-15 m \\
\frac{1}{600} x>10 m \\
x>6000 m
\end{gathered}
$$

This inequality says that if more than 6000 m texts are sent during the time the plan is bought for, it's best to get Plan B. Divide both sides by $m$ to get the number of texts per month.

$$
\frac{x}{m}>6000
$$

Therefore, if the number of texts sent per month is greater than 6000 , it's best to get Plan B.

